

# Motor Drive Dynamic System Model

Thermal Transient, Electronics, Controls

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# Summary

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A Dynamic (Time Domain) Simplorer Model of a Motor Drive:

- Electrical System Model
- Power Circuit
- Motor
- Controls
- Transient Thermal Model
- Simulation Results

Purpose:

- Simulate Transient Thermal Performance
- Determine Transient Ratings for the Motor Drive

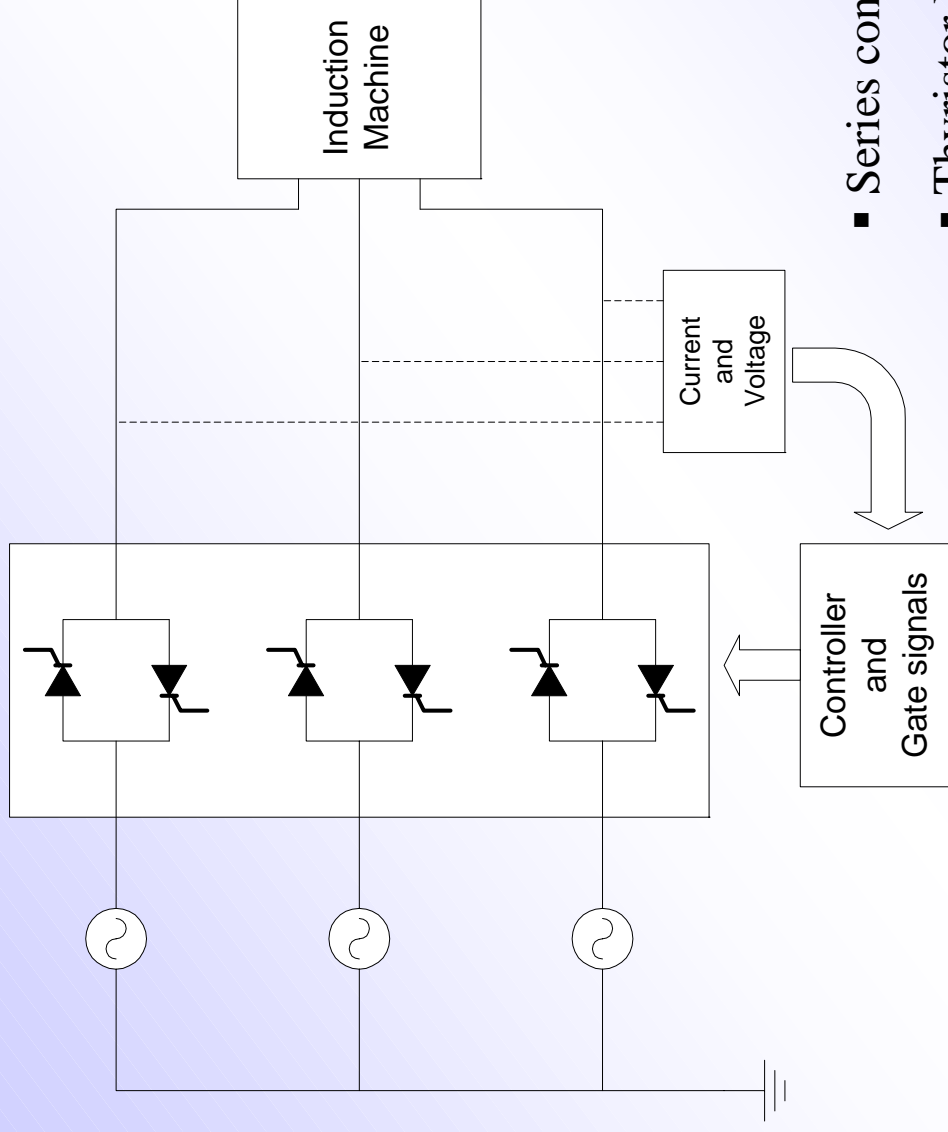
# Electrical System Model

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- Power Circuit Diagram
- Motor Model
- Control Model
- Verification

# Power Circuit Diagram

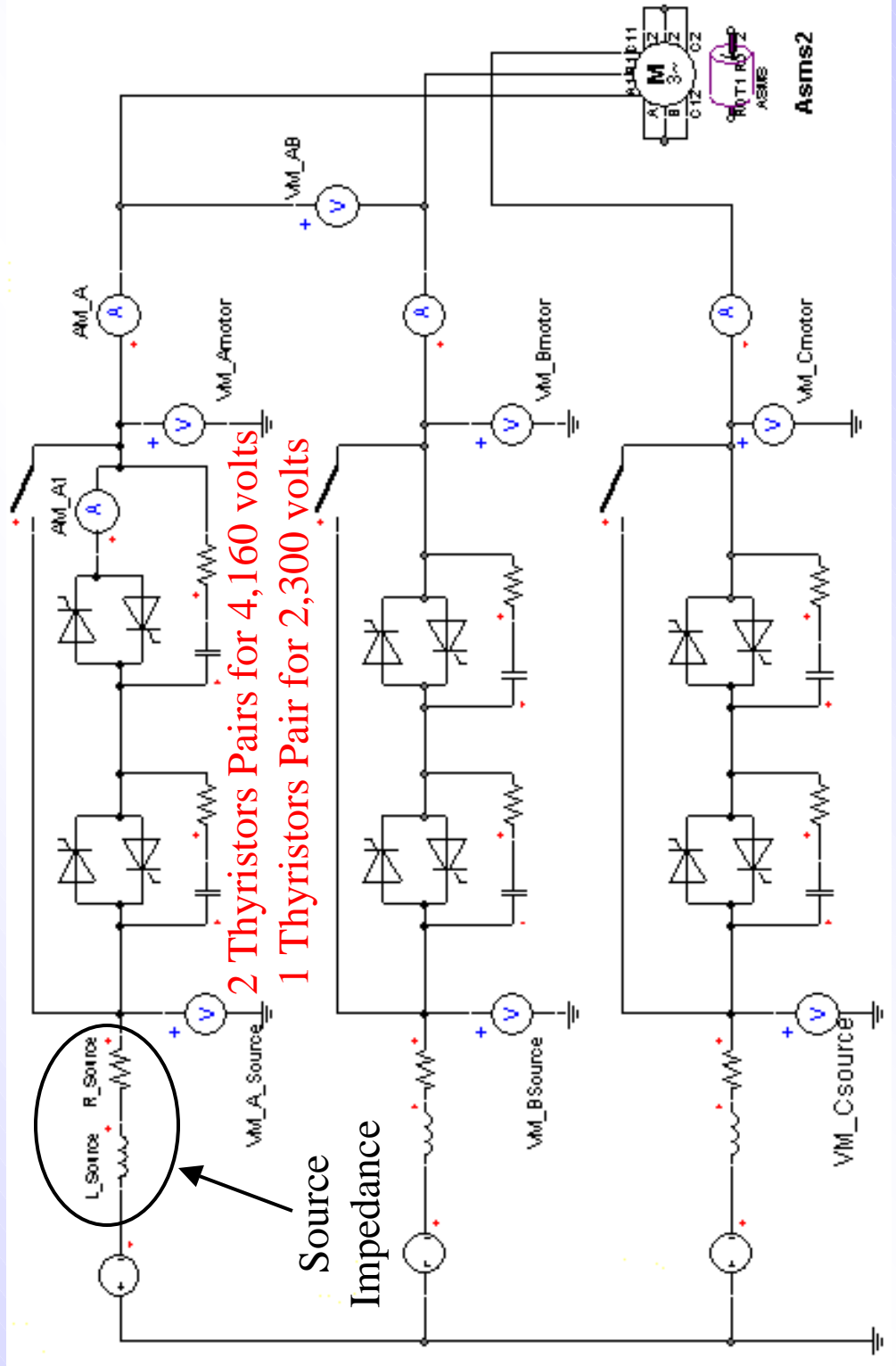
Soft Start is a Reduced Voltage method of Starting Induction Machines



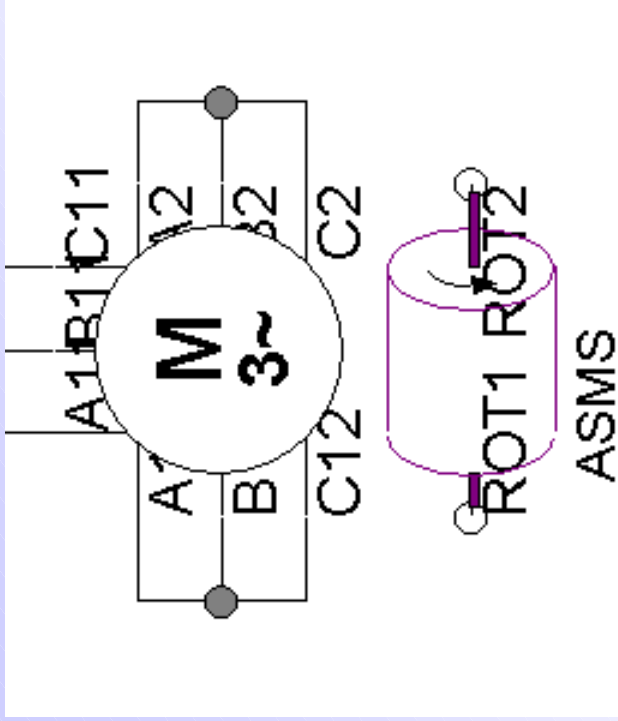
- Series connected back-to-back Thyristors
- Thyristor Pairs are Fired based on Current Zero
- The Firing Angle Profile is User Defined

# Overall Power Circuit

**Bypass Contactor**  
 Closes after the Motor is up to Speed  
 (Sensed by Thyristor Voltage, which typically Drops below Line Voltage)



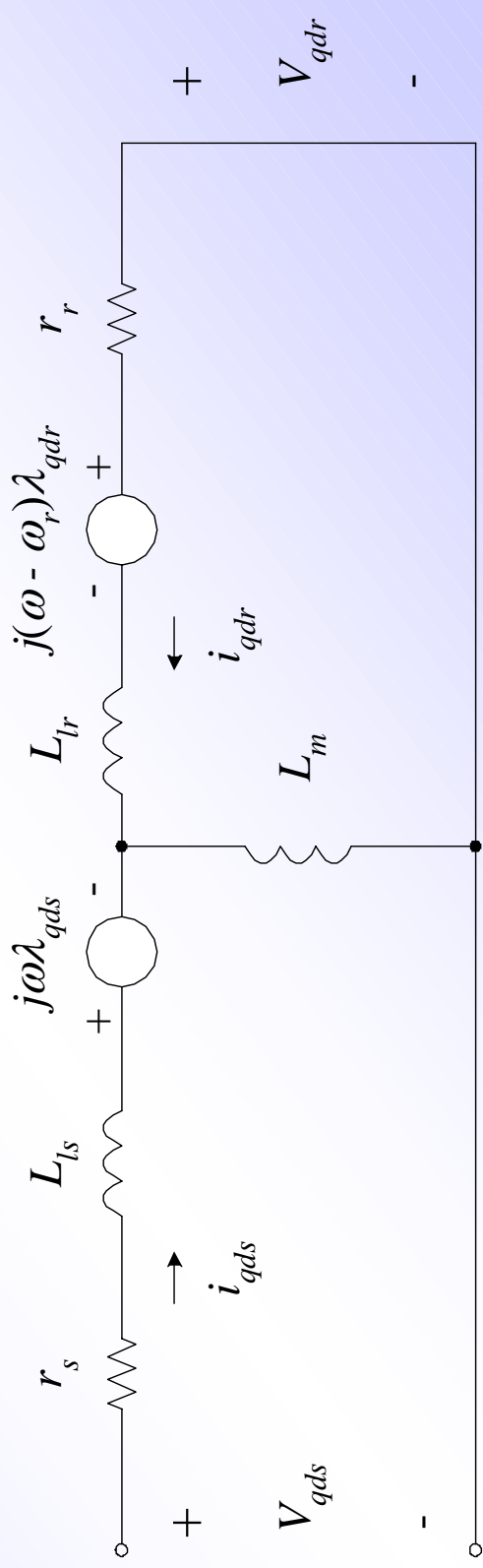
# Induction Motor Model



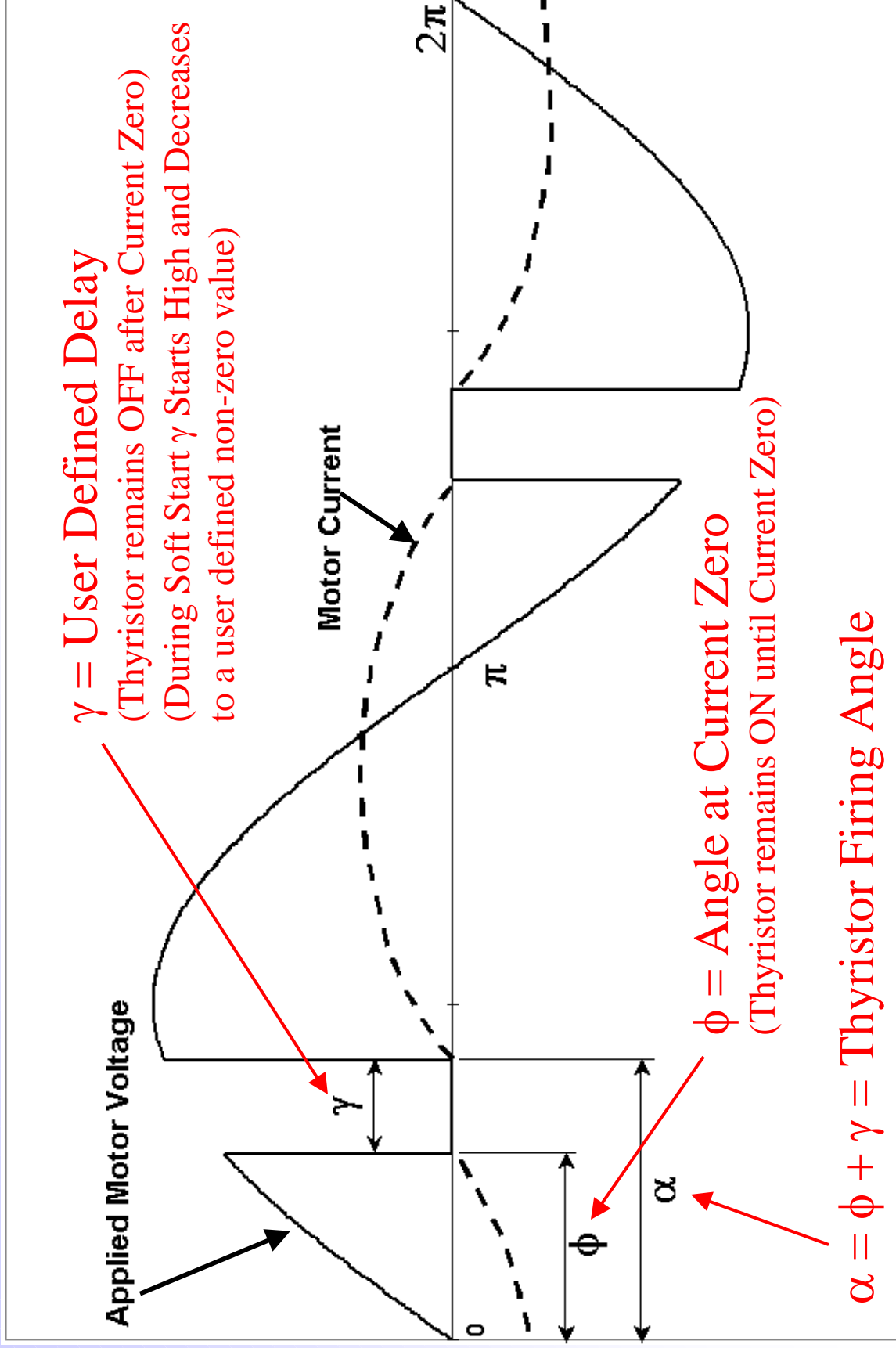
1000 hp, 4160 V, 60 Hz, 4-pole Motor Parameters

$$r_s = 0.348 \, \Omega \quad r_r = 0.348 \, \Omega \quad L_{ls} = 4.613 \, \text{mH}$$

$$L_{lr} = 4.613 \, \text{mH} \quad L_m = 246 \, \text{mH} \quad J = 31.4 \, \text{kg-m}^2$$



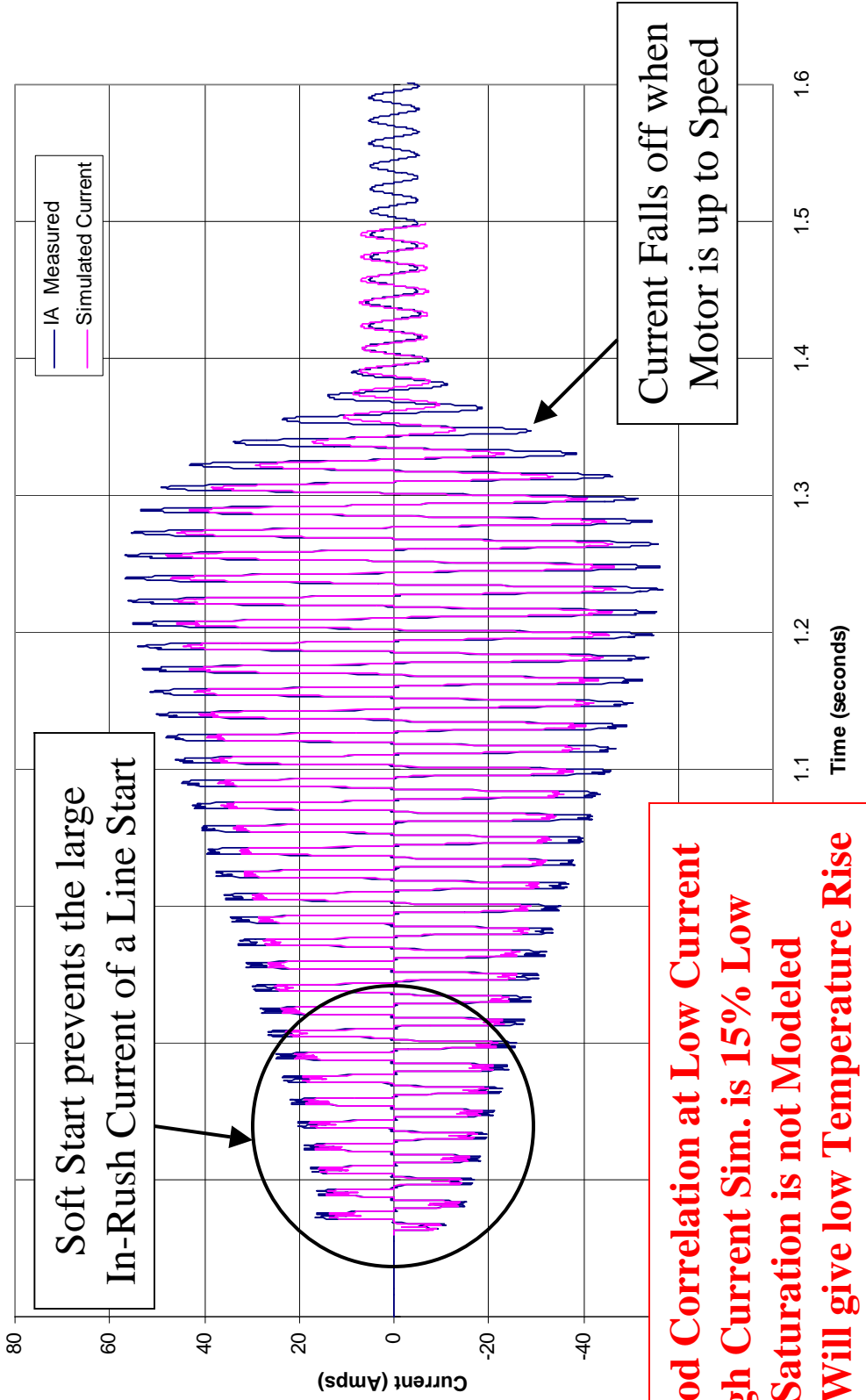
# Firing Angle Control



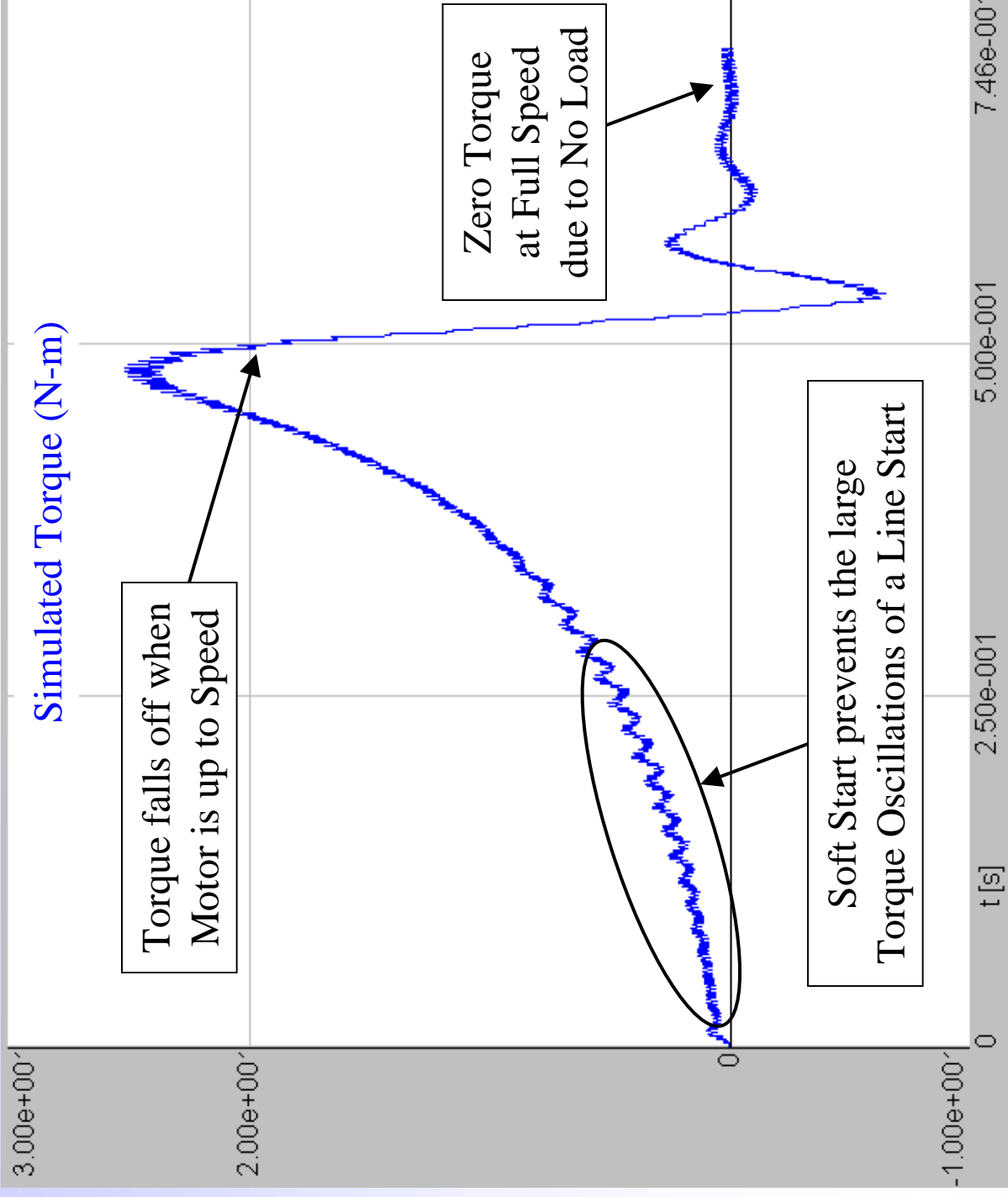


# Results - 5 Horsepower Motor (No Load)

Measured and Simulated Current (Amps)



# Results - 5 Horsepower Motor (No Load)

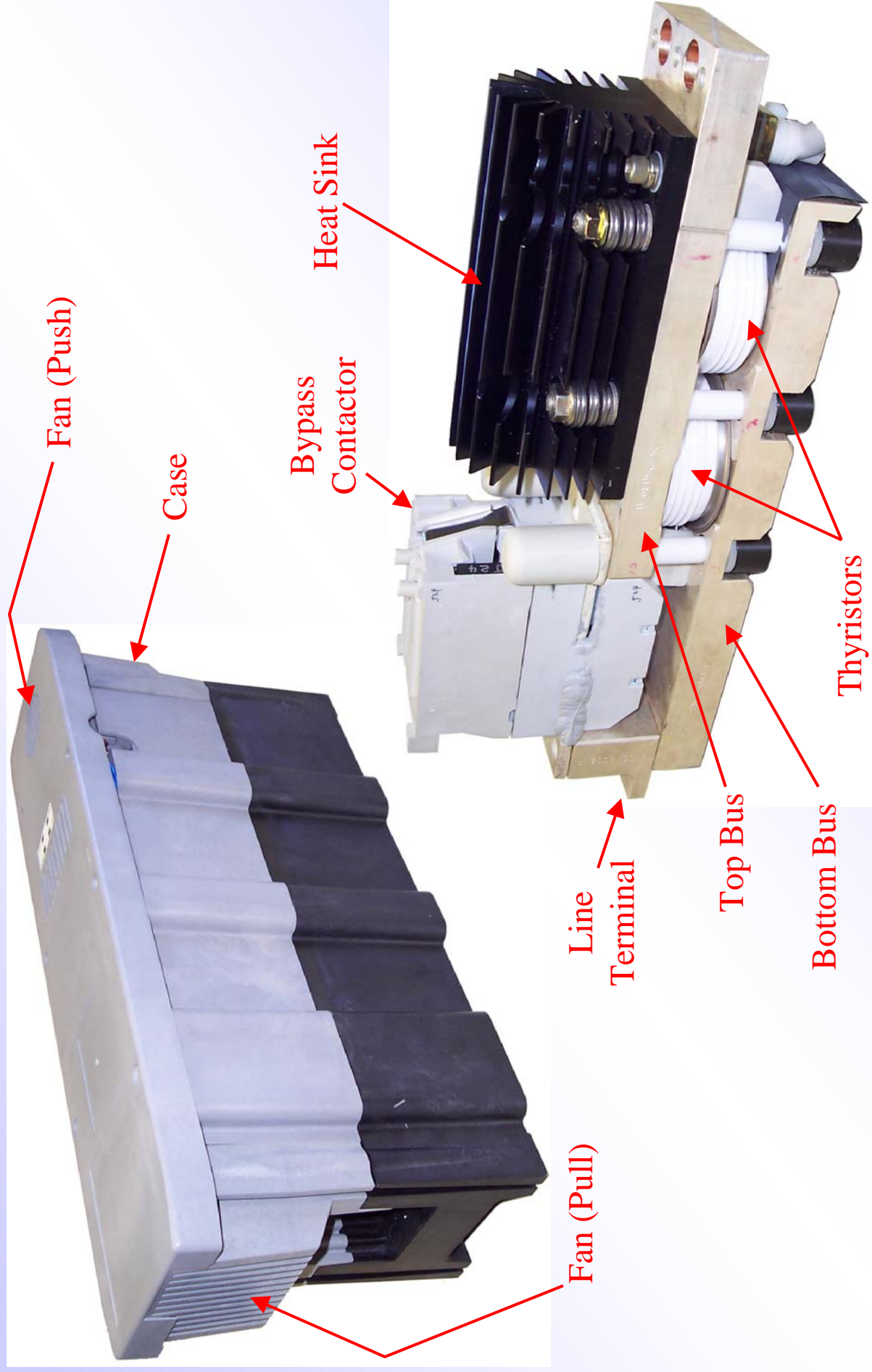


# Transient Thermal Model

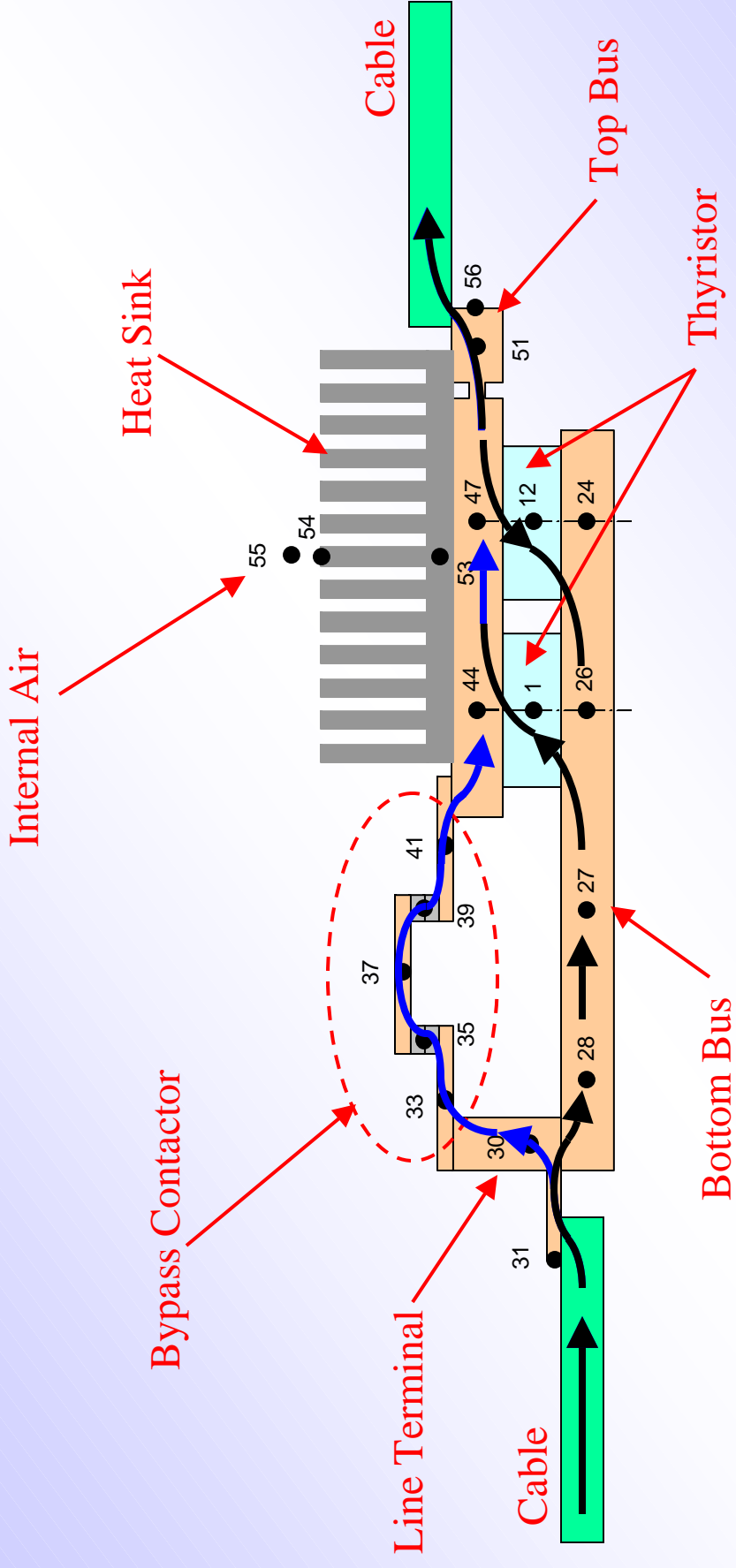
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- Electrical Analogy for Heat Transfer
  - Thermal Resistance
  - Thermal Capacitance
- Thermal Resistance - Heat Transfer
  - Conduction
  - Contact Interface
  - Convection
  - Radiation
  - Air Flow
- Thyristor - Transient Thermal Model
- Overall Motor Drive - Transient Thermal Model

# Soft Starter (one pole)

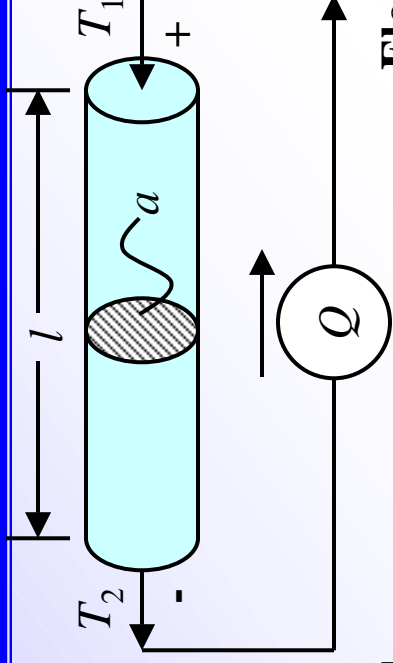


# Physical Schematic for Thermal Model



<u>Configuration</u>	<u>Soft Start</u>	<u>Full Speed</u>
• Bypass Contactor =	Open	Closed
• Current through =	Thyristors	Bypass Contactor

# Thermal Model - Electrical Analogy



## Thermal

Ohm's Law:

$$\Delta T = Q R_k$$

Conduction  
Resistance:

$$R_k = \frac{\Delta T}{Q} = \frac{l}{k a}$$

Capacitance:

$$Q = C_T \frac{dT}{dt}$$

## Electrical

$$\Delta V = I R_e$$

$$R_e = \frac{\Delta V}{I} = \frac{l}{\sigma a}$$

$$I = C_e \frac{dV}{dt}$$

Equivalent

$\Delta T$  = Temperature Drop ( $^{\circ}\text{C}$ )

$\Delta V$  = Voltage Drop (volt)

Terminologies:

$Q$  =  $I^2 R_e$  = Heat Source (watt)

$I$  = Current Source (amp)

$R_k$  = Resistance ( $^{\circ}\text{C}/\text{w}$ )

$R_e$  = Resistance (ohm)

$C_T$  =  $m c_p$  = Capacitance ( $\text{J}/^{\circ}\text{C}$ )

$C_e$  = Capacitance (farad)

$k$  = Conductivity ( $\text{w}/\text{m}^{\circ}\text{C}$ )

$\sigma$  = Conductivity ( $1/\text{ohm}\cdot\text{m}$ )

$m$  = Mass (kg)

$c_p$  = Specific Heat ( $\text{J}/\text{kg}\cdot^{\circ}\text{C}$ )

# Thermal Resistance

Radius of Contact Spot  
 $F = \text{Force (N)}$   
 $H = \text{Hardness (kg/mm}^2\text{)}$   
 $g = \text{gravity (9.8 m/s}^2\text{)}$

$$r_s = \sqrt{\frac{F}{\pi g H}}$$

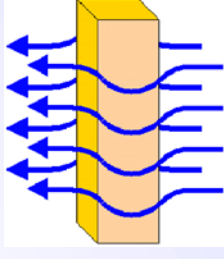
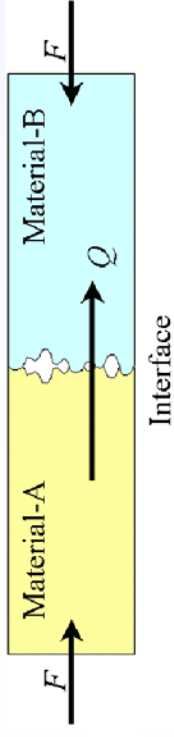
Solid Contact Spot

Voids between Surfaces

$$R_V = \frac{l_V}{k_V a_V}$$

$$R_I = \frac{1}{1/R_S + 1/R_V}$$

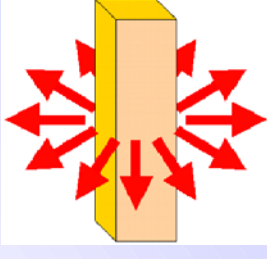
Total



Typical Convection Heat Transfer Coefficient  
 $h_c = 5 \text{ w/m}^2 \text{ }^\circ\text{C}$  ... Natural Convection for Air  
 $h_c = 12 \text{ w/m}^2 \text{ }^\circ\text{C}$  ... Forced Convection For Air

Convection:

$$R_c = \frac{1}{h_c a}$$



Typical Radiation Heat Transfer Coefficient  
 $h_r = 6 \text{ w/m}^2 \text{ }^\circ\text{C}$  ... for Electronic Systems

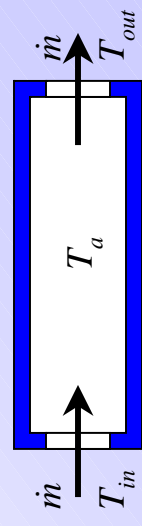
Radiation:

$$R_r = \frac{1}{h_r a}$$

$\Delta T_a = Q R_a$  ... Ave. Temperature Rise of Air Flow

$\dot{m} = \text{Air Mass Flow Rate (kg/s)}$

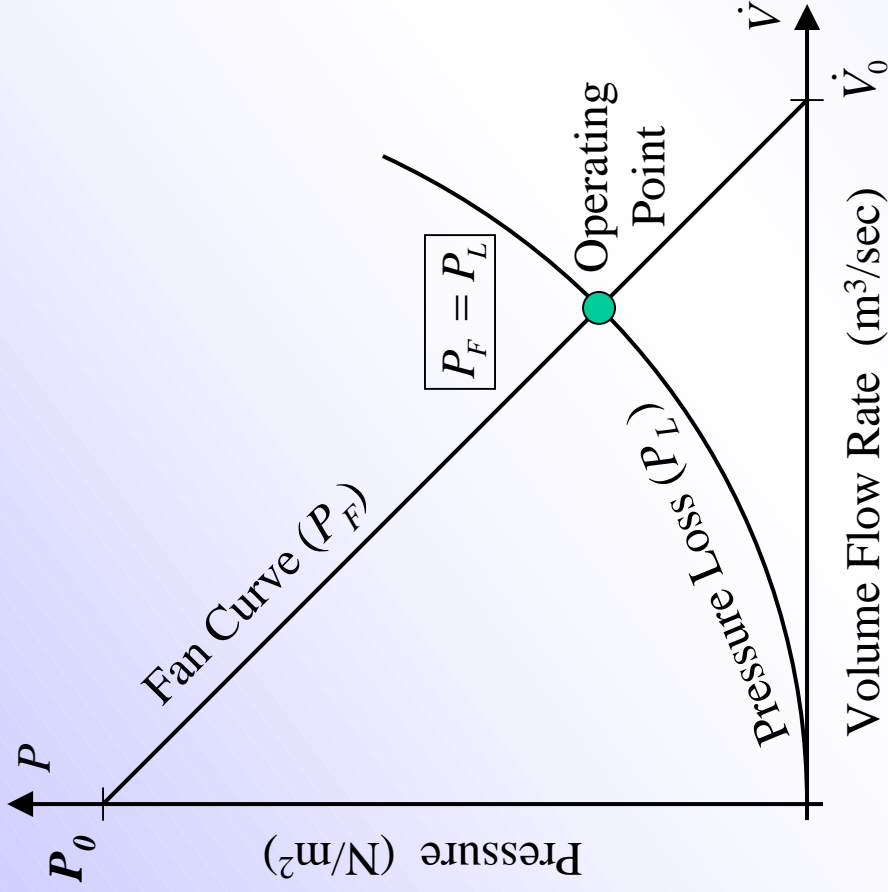
$c_p = \text{Specific Heat of Air}$



Air Flow:

$$R_a = \frac{1}{2 \dot{m} c_p}$$

# Air Flow



## Fan Curve:

$$P_F = P_0 - \frac{P_0 \dot{V}}{V_0} = P_0 - \frac{P_0}{\dot{m}_0} \dot{m}$$

## Pressure Loss across Vents and Turns:

$$P_L = C_L \frac{\rho u^2}{2} = C_L \frac{\dot{m}^2}{2\rho A^2} = \frac{\dot{m}^2}{2} \sum \frac{C_L}{\rho A^2}$$

$u$  = Air Velocity (m/s)

$\rho$  = Air Density (kg/m<sup>3</sup>)

$\dot{m}$  = Air Mass Flow Rate (kg/s)

$A$  = Air Path Cross Sectional Area (m<sup>2</sup>)

$C_L$  = Loss Coefficient

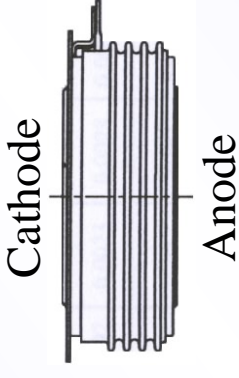
Sudden Contraction:  $C_L = 0.5$

Sudden Expansion:  $C_L = 1.0$

90° Turn:  $C_L = 1.5$

# Thyristor - Data Sheet

		Values from the T-501N data sheet				
Both Sides		1	2	3	4	5
Ri	C/w	0.00033	0.00272	0.00304	0.00243	0.00848
TCi	s	0.0019	0.0134	0.062	0.132	0.676
Anode Side		1	2	3	4	5
Ri	C/w	0.0192	0.0023	0.0028	0.00366	0.00254
TCi	s	4.13	0.4	0.154	0.0607	0.0101
Cathode Side		1	2	3	4	5
Ri	C/w	0.0281	0.00106	0.00487	0.00237	0.0021
TCi	s	4.13	0.45	0.126	0.0374	0.0091

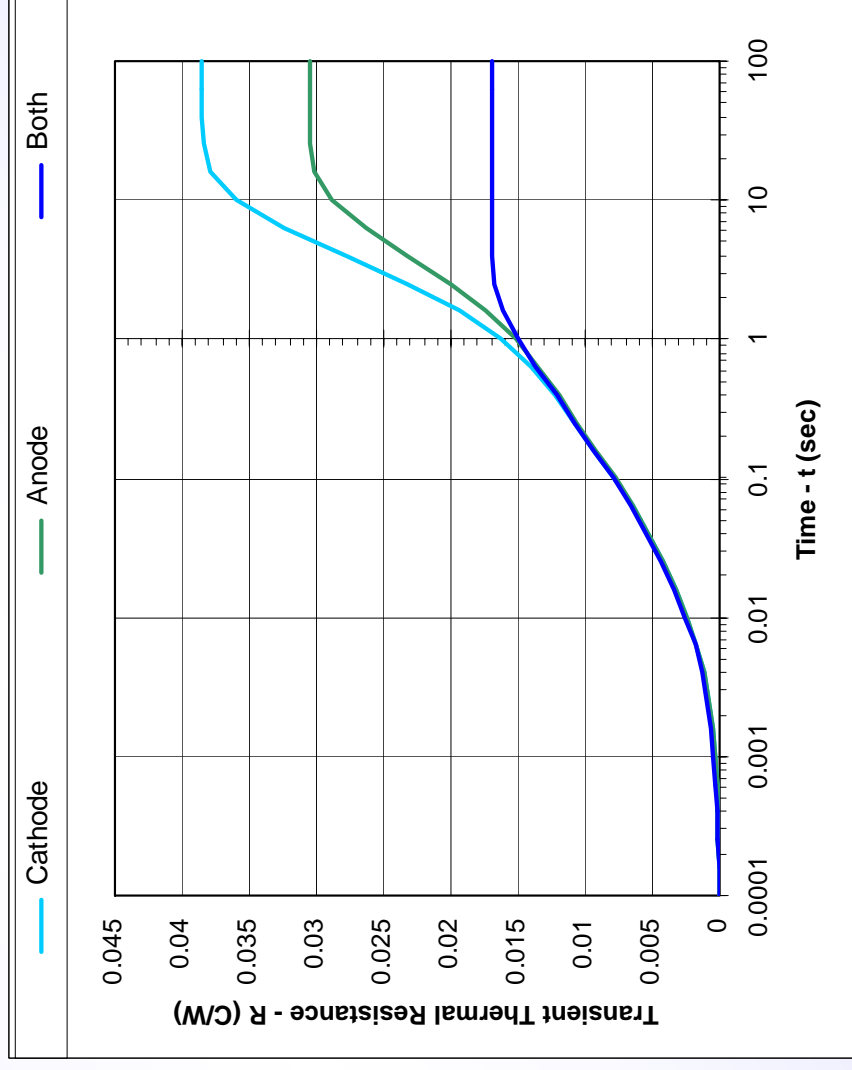


$$R = \sum_{i=1}^5 R_i (1 - e^{-t/TC_i})$$

## Transient Thermal Resistance

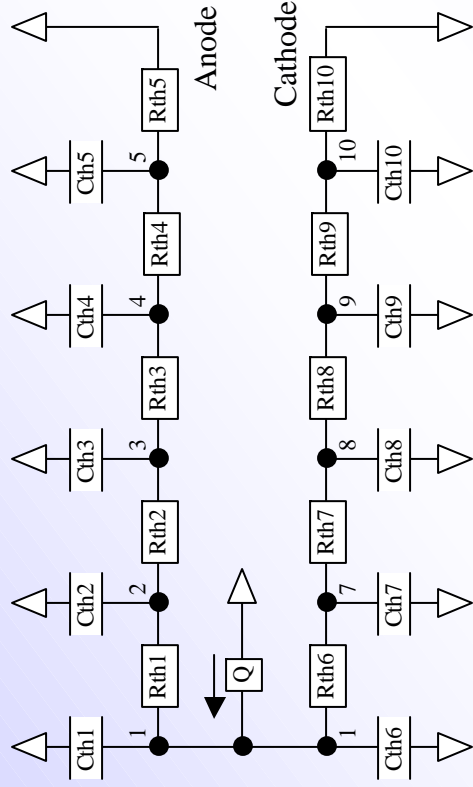
**Valid** only when the Thyristor is continuously “ON”.

**NOT Valid** when the Thyristor is switched “ON” and “OFF” repeatedly.

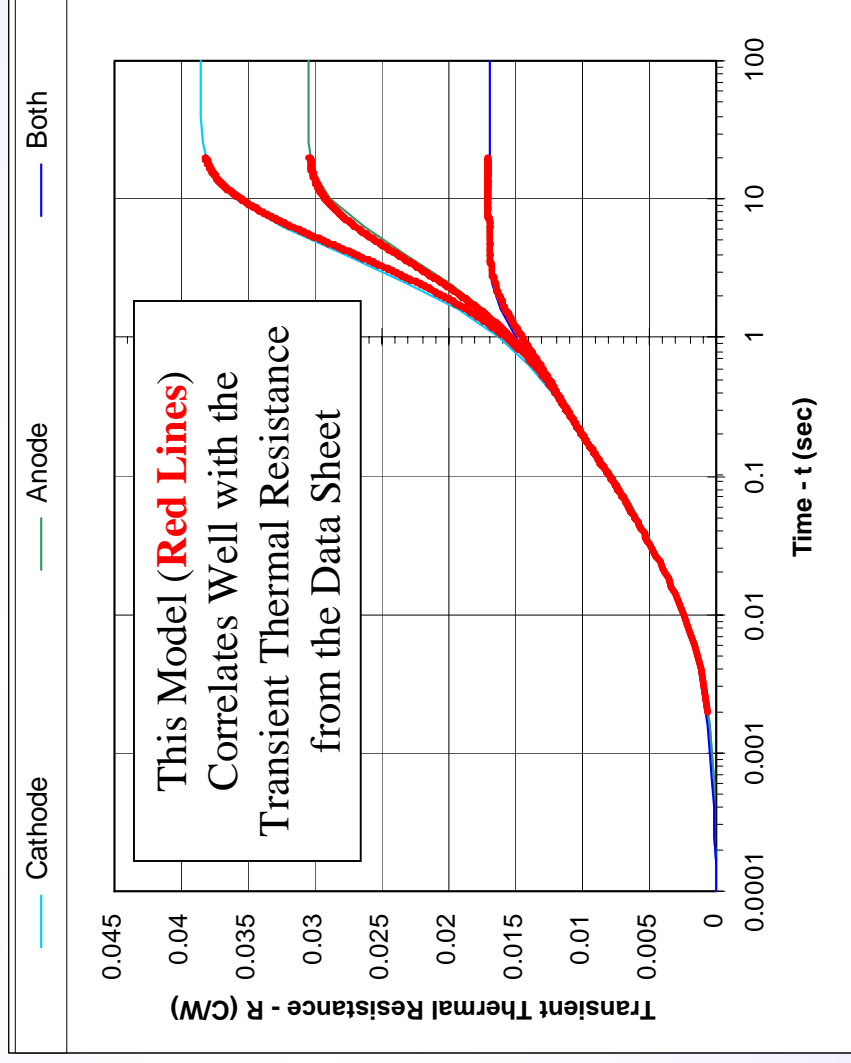


# Thyristor - Thermal Model

## Thermal Resistance and Capacitance Model

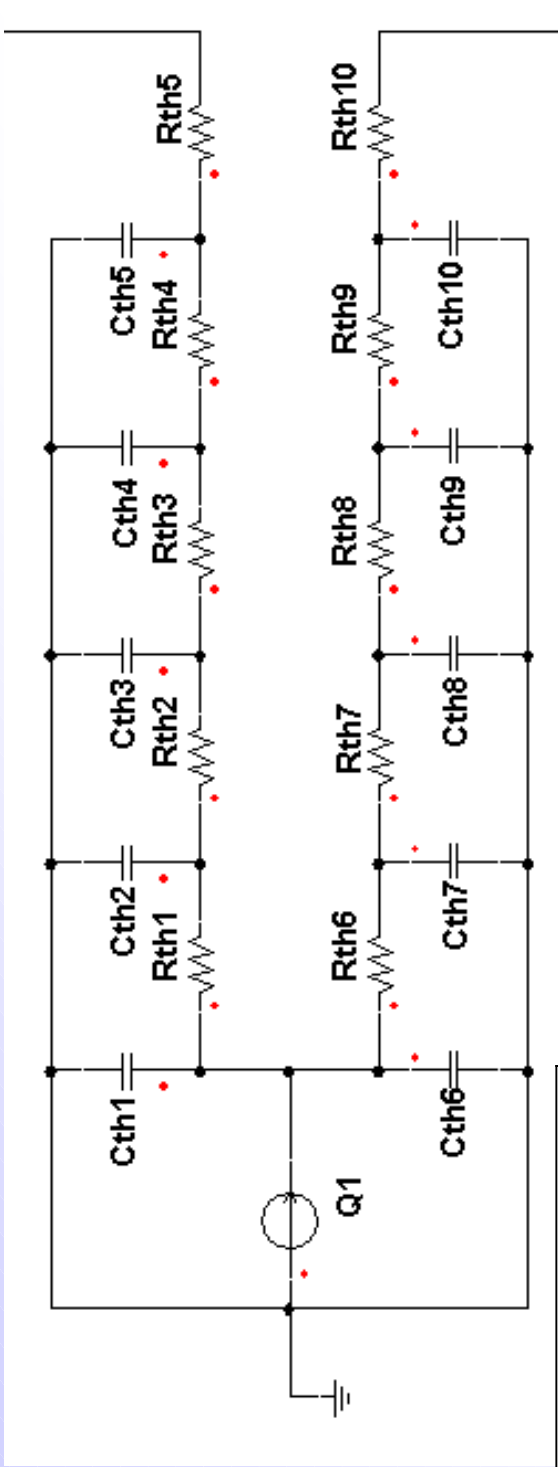


R-C Network - for the T501N - - Input Values					
Anode Side	1	2	3	4	5
Rth	0.0015	0.004	0.005	0.01	0.01
Cth	1.28	0.2	0.3	10	60
TCth	s	0.0019	0.0008	0.1000	0.6000
Cathode Side	6	7	8	9	10
Rth	0.0015	0.004	0.005	0.013	0.015
Cth	1.28	0.2	0.3	5	60
TCth	s	0.0019	0.0008	0.0650	0.9000



**Valid** for All Conditions  
including “ON / OFF” switching.

# Thyristor Thermal Model in Simplorer



The Thyristor Heat Source is modeled as a Current Source

Properties - Q1 - Current Source

The Heat Source is calculated from the Thyristor Voltage Drop and Current

Parameters | AC - Parameters | Output / Display | Library

Name: Q1

Parameters:  Source Current [A] TH1.V\*TH1.I

Show Name

Use Pin

Value, Variable, Expression

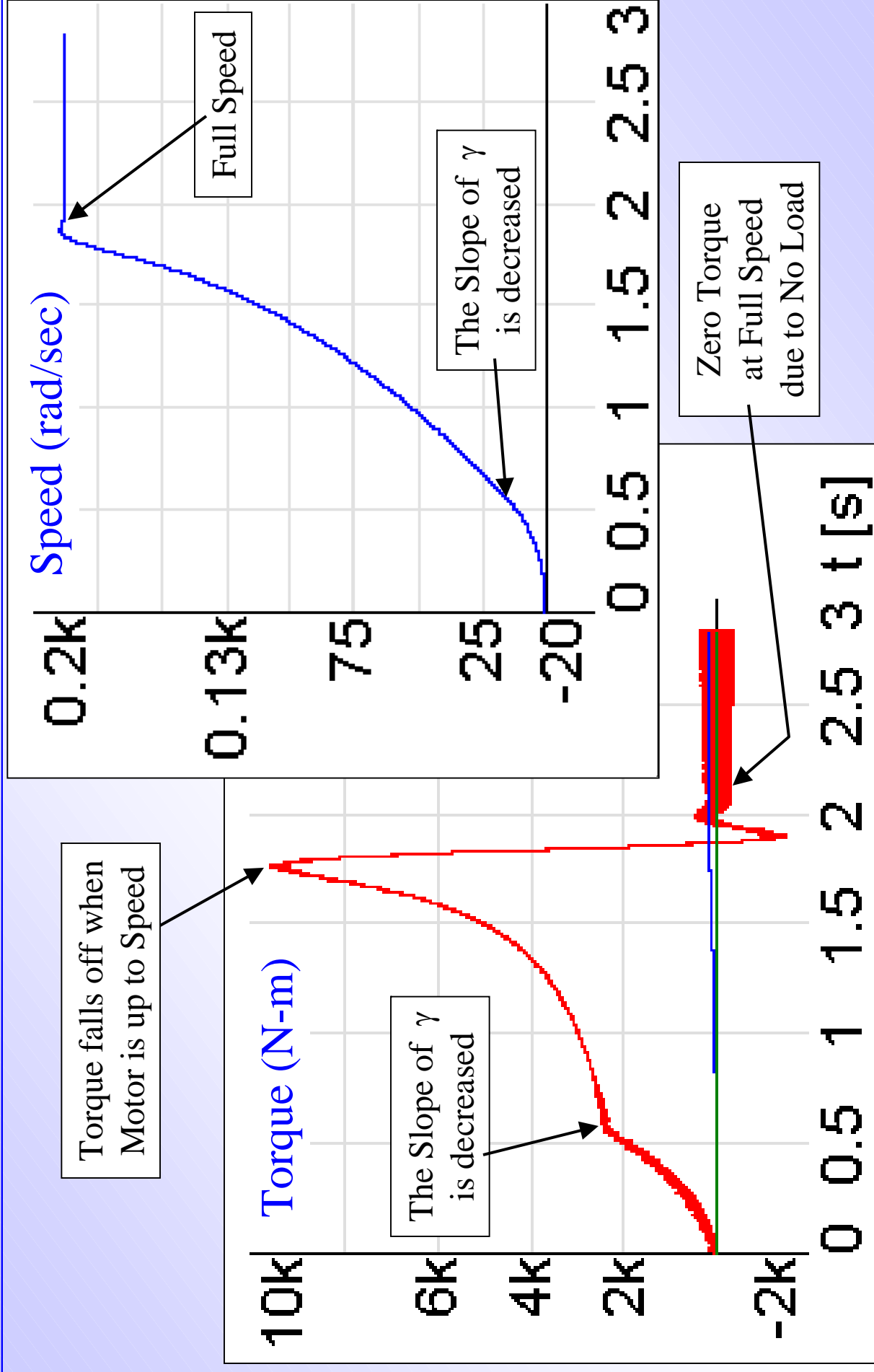


# Simulation Results

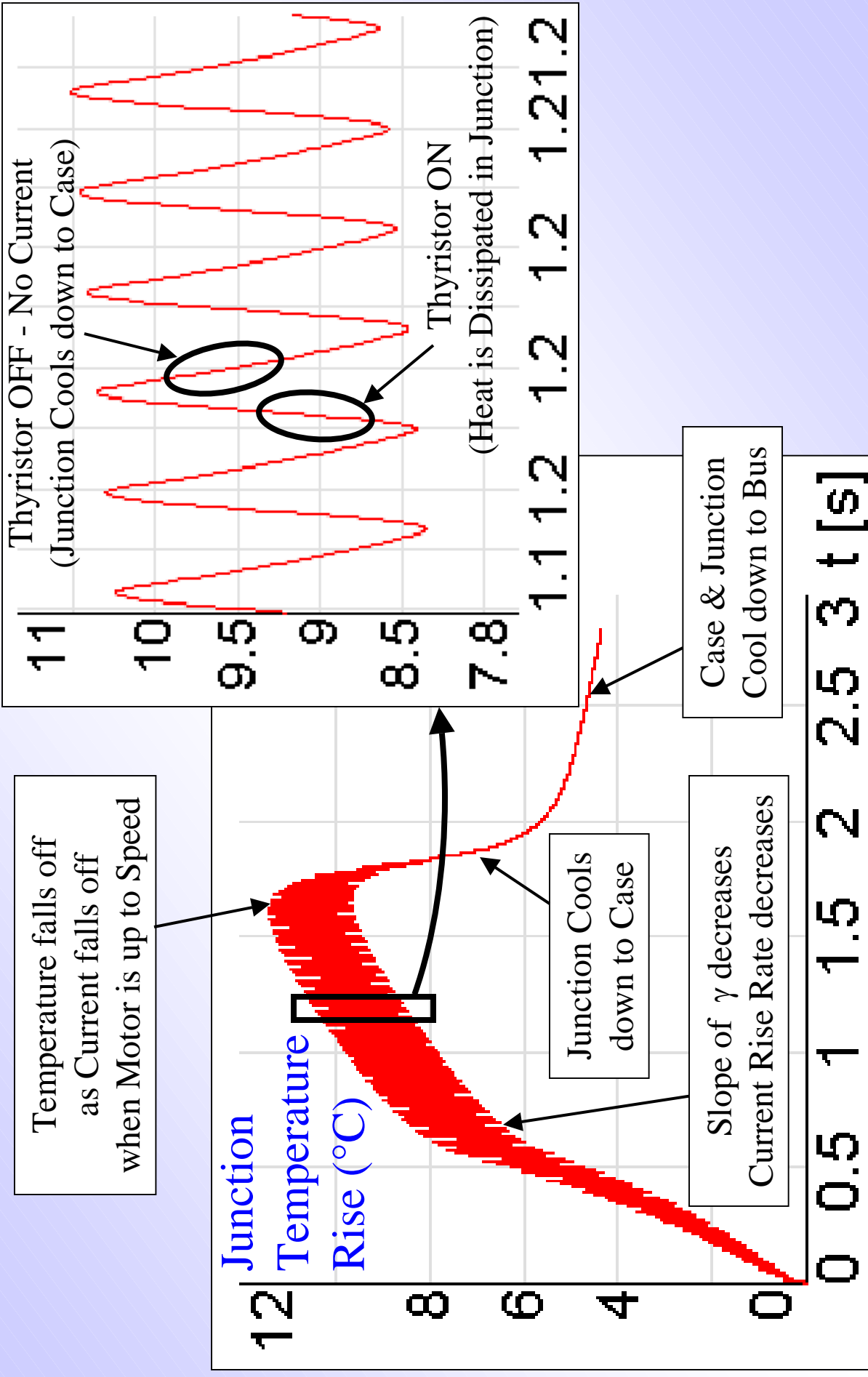
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- Current vs. Time
- Temperature vs. Time

# Results - 1,000 Horsepower Motor (No Load)



# Results - 1,000 Horsepower Motor (No Load)



# Summary & Conclusions

Presented a Simplorer Dynamic Model of a Motor Drive:

- Electrical System Model
  - Power Circuit, Motor, Control
- Transient Thermal Model
  - Electrical Analogy, Thermal Resistance, Thermal Capacitance, Air Flow

Presented Simulation Results:

- Verification of the Electrical System Model
- Simulation Results for a 1000 Horsepower Motor
  - Transient Electrical & Transient Thermal Performance

Future Work:

- Verify the Transient Thermal Model against Tests
- Use this Model to determine the Transient Ratings of the Drive
  - Cycling: Start - Run - Stop .... Start - Run - Stop .... Start - Run - Stop
  - Different Motor & Load Combinations